Warm-up

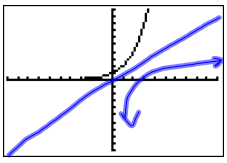
Find the inverse.

1. y = 2x - 3

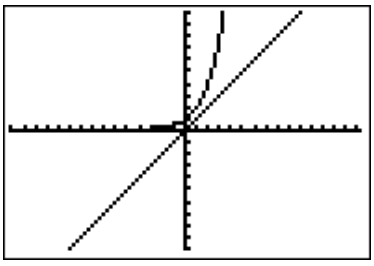
2. $y = \sqrt[3]{2x}$

10-2 Logarithms and Logarithmic Functions

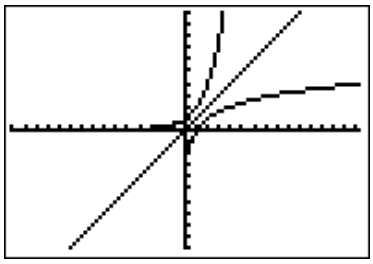
$y = 2^x$



Does this graph have an inverse?



Does this graph have an inverse?



$y = 2^x$ $y = \log_2 x$ "log base 2 of x"

Inverses of each other

$y = b^x$ $y = \log_b x$

What is the inverse?

$y = 10^x$

Characteristics of a Logarithmic Function

1. The function is continuous and one-to-one.
2. The domain is the set of all positive real numbers.
3. The y-axis is an asymptote of the graph.
4. The range is the set of all real numbers.
5. The graph contains the point $(1, 0)$. That is, the x-intercept is 1.

Suppose b and x are positive, and $b \neq 1$, then, there is a number y such that:

$$\log_b x = y \text{ iff } b^y = x$$

(Used to convert between logarithmic and exponential form.)

$$\log_b x = y \text{ iff } b^y = x$$

Logarithmic Form	Exponential Form
$\log_2 16 = 4$	$2^4 = 16$
$\log_2 8 = 3$	$2^3 = 8$
$\log_2 1 = 0$	$2^0 = 1$
$\log_2 x = y$	$2^y = x$
$\log_b x = y$	$b^y = x$

$$\log_b x = y \text{ iff } b^y = x$$

Logarithmic Form	Exponential Form
$\log_{10} 1000 = 3$	
$\log_{16} 4 = .5$	
$\log_3 27 = 3$	
$\log_9 81 = 2$	

Evaluate a logarithmic expression.

ex $\log_2 64 = y$

$2^y = 64$

$2^y = 2^6$

$y = 6$

ex $\log_{25} 5 = y$

$25^y = 5$

$5^{2y} = 5^1$

$\frac{1}{2}$

ex $\log_{10} 0.1$

Remember:
Two functions are inverses iff
$[f \circ g]\, x = x$ and $[g \circ f]\, x = x$

Inverses of each other

$y = b^x$ $\quad y = \log_b x$

$f(x) = b^x$ $\quad g(x) = \log_b x$

$$b^{\log_b x} = x$$

Properties of logs

$$\log_b b^x = x$$

ex
$\log_2 2^5$

5

ex
$\log_4 4^2$

2

ex
$\log_7 49$

2

ex
$3^{\log_3 5}$

5

ex
$8^{\log_8 10}$

10

DO:

1. $\log_{\frac{1}{2}} 32$
2. $\log_9 27$
3. $\log_5 125$
4. $\log_8 4$
5. $9^{\log_9 5}$
6. $\log_{\sqrt{3}} 9\sqrt{3}$

p536
21-31odd
33-44